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## Actuarial Certification


#### Abstract

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[^0]stoneconsulting,inc

October 5, 2017
Lawrence Retirement Board
354 Merrimack Street
Suite 302
Lawrence, MA 01843
Dear Members of the Board:

For the purpose of satisfying the requirements of the Government Accounting Standards Board (GASB) Statements No. 67 and 68, Stone Consulting, Inc. has prepared a set of illustrative tables and other Required Supplementary Information (RSI) based on the January 1, 2016 actuarial valuation of the Lawrence Retirement System performed by Stone Consulting, Inc. The valuation and this report were prepared using generally accepted actuarial principles and practices and meet the parameters set by the Governmental Accounting Standards Board (GASB).

For GASB 67 the results are as of a valuation date of January 1, 2016 and a reporting date of December 31, 2016. For GASB 68 the results are as of a valuation date of January 1, 2016, a measurement date of December 31, 2016 and a reporting date of June 30, 2017. To the best of our knowledge, this report is complete and accurate, and the assumptions used represent our best estimate of anticipated experience of the system. The methods, assumptions, and plan provisions used to prepare these exhibits are consistent with those used in the funding valuation, and are outlined in the January 1, 2016 funding valuation report unless otherwise stated in this report.

We are pleased to present these exhibits. If the Lawrence Board has any questions on the content of this report, we would be glad to respond. Please note that this report is meant to be used in its entirety. Use of excerpts of this report may result in a misleading or inaccurate understanding of the results.

The undersigned is a consultant for Stone Consulting, Inc. and a member of the American Academy of Actuaries and meets the Qualification Standards of the American Academy of Actuaries to render the actuarial opinion contained herein.

Respectfully submitted,
STONE CONSULTING, INC.
Actuaries for the Plan

Lawrence B. Stone
Member, American Academy of Actuaries

## GASB Statements No. 67 and 68 - Net Pension Liability

The components of the Net Pension Liability of the Lawrence Retirement System as of December 31, 2016 were as follows:

| Total Pension Liability (TPL) |  | $\$$ | $418,089,045$ |
| :--- | ---: | ---: | ---: |
| Plan Fiduciary Net Position (FNP) |  | $\$$ | $195,465,910$ |
| System's Net Pension Liability (NPL) |  | $222,623,135$ |  |
| Plan FNP as a percentage of the TPL |  | $46.8 \%$ |  |
| Covered Payroll | $\$ 3,741,641$ |  |  |
| Plan NPL as a percentage of Covered Payroll |  | $301.9 \%$ |  |

NOTE: Totals in this report may not sum due to rounding
Changes to the Net Pension Liability [GASB 68, Paragraph 44]

|  | Total Pension Liability <br> (a) | Plan Fiduciary Net Position <br> (b) | Net Pension Liability <br> (a) - (b) |
| :---: | :---: | :---: | :---: |
| Balances at beginning of Measurement Period (01/01/2016) | \$ 415,175,624 | \$ 182,660,273 | \$ 232,515,351 |
| Changes for the Year: |  |  |  |
| Service Cost | 8,737,363 |  | 8,737,363 |
| Interest | 31,842,170 |  | 31,842,170 |
| Change in benefit terms | 0 |  | 0 |
| Differences between expected and actual experience | $(11,573,571)$ |  | $(11,573,571)$ |
| Change in assumptions | 0 |  | 0 |
| Contributions - employer |  | 19,329,195 | $(19,329,195)$ |
| Contributions - employee |  | 6,851,473 | $(6,851,473)$ |
| Net investment income |  | 13,190,264 | $(13,190,264)$ |
| Benefit payments, including refunds of employee contributions | $(26,092,541)$ | $(26,092,541)$ | 0 |
| Administrative expense |  | $(472,754)$ | 472,754 |
| Other changes |  | 0 | 0 |
| Net Changes | 2,913,421 | 12,805,637 | $(9,892,216)$ |
| Balances at end of Measurement Period (12/31/2016) | \$ 418,089,045 | \$ 195,465,910 | \$ 222,623,135 |

Update procedures were used to roll the Total Pension Liability forward from the valuation date $(01 / 01 / 2016)$ to the measurement date (12/31/2016). [GASB Statement No. 68, Paragraph 45 a.]

## Projection of the Net Pension Liability

## TOTAL PENSION LIABILITY (TPL)

The Total Pension Liability at the beginning of the measurement period ( $01 / 01 / 2016$ ) is equal to the TPL from the end of the end of the previous measurement period, and is then compared to the Actuarial Accrued Liability calculated as of that date. GASB Statement No. 68, Paragraph 32 requires that the AAL be calculated under the Entry Age Normal Cost Method. Any changes since the prior valuation in assumptions or plan provisions are calculated, and the remainder of any difference between the projected TPL and the Accrued Liability is recognized as "Differences between actual and expected experience".

The TPL is projected to the end of each measurement period (12/31/2016) by adding all of the changes resulting from experience, assumption changes, and changes to plan provisions. Interest is given to the TPL, Service Cost, and paid benefits, and added to the total, less the projected benefit payments for the year. Changes due to expected and actual gains on pension plan assets will be recognized over a five-year period [GASB Statement No. 68, Paragraph 33b], and liabilities arising from experience or changes in assumptions will be spread over the lifetime of the current employees [GASB Statement No. 68, Paragraph 33a].

The TPL shown is different from the AAL shown in the January 1,2016 actuarial valuation report. This is due to a different treatment of net 3(8)(c) payments. In the funding valuation we fund the net 3(8)(c) payments on a pay-as-you-go basis. For GASB Statements No. 67 and 68 we have developed a liability amount of \$6,402,782, which we have added to the funding AAL as of January 1, 2016 to derive the Total Pension Liability. The liability is calculated by assuming that every dollar of 3(8)(c) net benefit generates the same amount of liability as a dollar of the total retirement benefit.

## PLAN FIDUCIARY NET POSITION (FNP)

GASB Statement No. 68, Paragraph 20 requires that Market Value of Assets be used for the Fiduciary Net Position. Net investment income is the portion of the change in assets during the measurement period not attributed to employee/employer contributions, benefits payments, administrative expense, or other changes.

The projected Net Pension Liability (NPL) for the end of the year is the portion of the TPL not covered by the FNP. This amount is presented as a percentage of covered employee payroll. The NPL ratio for Lawrence is $301.9 \%$ of covered payroll. In this report, covered payroll is reported as described in GASB Statement No. 82. It is a projected pensionable payroll for the measurement period.

## Distribution of the Member Population

As of January 1, 2016, the following employees were covered by the benefits terms:

| Inactive employees or beneficiaries currently receiving benefits | 887 |
| :--- | ---: |
| Inactive employees entitled to a return of contributions | 382 |
| Active employees | 1,600 |
| TOTAL | 2,869 |

Pension Expense and Deferred Outflows of Resources and Deferred Inflows of Resources Related to Pensions [GASB 68, Paragraph 44 h.]

|  | Deferred Outflows <br> Of Resources |  | Deferred Inflows <br> Of Resources |
| :--- | :---: | :---: | :---: |
| Differences between expected and actual experience <br> Changes of assumptions | $\$$ | 0 | $\$ 8$ |
| Net difference between projected and actual earnings <br> on pension plan investments <br> Total | 0 | 0 | 0 |


| Year Ending December 31, * | Recognition |
| :---: | ---: |
| 2017 | $\$ \quad 1,197,125$ |
| 2018 | $1,197,125$ |
| 2019 | $1,092,470$ |
| 2020 | $(1,511,996)$ |
| 2021 | $(1,677,329)$ |
| Thereafter | $(1,509,596)$ |

*The years are based on measurement date. For GASB 68, the year ending December 31, 2017 is Fiscal 2018.

## Development of Exhibits

## DISCOUNT RATE

Projections were made using a discount rate assumption of $7.75 \%$, which is consistent with the assumption used in the valuation. One of the objectives of the provisions introduced by GASB 68 is to examine how benefit payments and plan contributions and investment earnings interact on a cash flow basis. GASB requires that these amounts be calculated with Market Value of Assets and using the Entry Age Normal cost method.

Projected contributions for each year are the sum of the projected normal cost, the amortization of the unfunded liability, administrative expense, and other benefit costs such as 3(8)(c) payments. The amortization bases and periods are consistent with those seen in the valuation report. Administrative expenses are increased by $4.25 \%$ per year.

Lawrence's Fiduciary Net Position was projected to be available to make all future benefit payments of current active and inactive employees. Thus, the long-term expected rate of return on investments was applied for all benefit periods when calculating the Net Pension Liability.

The long-term rate of return which was used to develop the discount rate of $7.75 \%$ includes the effect of inflation (not subtracted out as in the real rates of return). It is based on a combination of expected rates of return on the mix of current and expected investments over a long-term period. These expectations are based on current market conditions, historical experience and future expectations. It assumes a rebalancing of assets on an ongoing basis as well as a constant monitoring of asset allocation and manager performance.

GASB Statement No. 67, Paragraph 30 b. 4 requires that a return rate for the measurement period be developed using the market value of assets at the beginning of the measurement period, along with monthly cash flows. This has been done for the 2016 calendar year, and is shown on the following page and on page 11.

| Calendar Year | 2016 |
| :---: | :---: |
| Money-Weighted Rate of Return | $7.53 \%$ |

## Discount Sensitivity [GASB 68, Paragraph 42 g.]

The following presents Lawrence's Net Pension Liability calculated at the valuation discount rate of 7.75\%, as well as at discount rates one percent higher (8.75\%) and one percent lower (6.75\%).

| Fiscal Year | $1 \%$ Decrease <br> $(6.75 \%)$ | Current Discount Rate <br> $(7.75 \%)$ | $1 \%$ Increase |
| :---: | :---: | :---: | :---: |
| 2017 | $\$ 273,136,374$ | $\$ \quad 222,623,135$ | $\$(8.75 \%)$ |

## Long-Term Expected Real Rate of Return

The long-term expected real rate of return reflects the expected rate of return on plan assets minus the expected rate of inflation. Note that the discount rate includes the effect of inflation. The long-term real rate of return removes the effect of inflation on the return amounts. It is a long-term assumption and is meant to reflect a best estimate of future experience, based on the expected asset allocation. The allocation percentages are based on information provided by the Lawrence Retirement System and PRIT's asset consultant, NEPC. The real rates of return below are based on 30-year return estimates provided by NEPC through the Pension Reserve Investment Trust, adjusted using a $3.00 \%$ inflation assumption.

| Asset Class | Target Allocation | Long-Term Expected Real Rate of Return (Geometric Average) |
| :---: | :---: | :---: |
| Large Cap Equities | 14.50\% | 4.37\% |
| Small/Mid Cap Equities | 3.50\% | 4.61\% |
| International Equities | 16.00\% | 4.69\% |
| Emerging Equities | 6.00\% | 6.42\% |
| Equities | 40.00\% | - |
| Core Bonds | 5.00\% | 0.97\% |
| 20+ Yr. Treasury STRIPS | 2.00\% | 0.73\% |
| TIPS | 5.00\% | 0.73\% |
| Core Fixed Income | 12.00\% | - |
| High-Yield Bonds | 1.50\% | 2.67\% |
| Bank Loans | 2.50\% | 2.91\% |
| EMD (External) | 1.00\% | 2.67\% |
| EMD (Local Currency) | 0.00\% | 3.40\% |
| Distressed Debt | 3.00\% | 5.88\% |
| Other Credit Opportunities | 2.00\% | 3.73\% |
| Value-Added Fixed Income | 10.00\% | - |
| Private Equity | 11.00\% | 6.31\% |
| Real Estate | 10.00\% | 3.40\% |
| Timberland | 4.00\% | 2.91\% |
| Hedge Funds / Portfolio Completion | 13.00\% | 3.38\% |

(Amounts in Thousands)


[^1](Amounts in Thousands)

| Fiscal Year | 2017 | 2016 | 2015 | 2014 | 2013 | 2012 | 2011 | 2010 | 2009 | 2008 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Actuarially determined contribution | \$ 19,320 | \$ 18,515 | \$ 17,121 |  |  |  |  |  |  |  |
| Contributions in relation to the actuarially determined contribution | $(19,329)$ | $(18,509)$ | $(17,033)$ |  |  |  |  |  |  |  |
| Contribution deficiency / (excess)* | (9) | 6 | 88 | * Information not available for years prior to 2015 |  |  |  |  |  |  |
| Covered-employee payroll | \$ 75,582 | \$ 74,625 | \$ 72,939 |  |  |  |  |  |  |  |
| Contributions as a percentage of covered-employee payroll | 25.6\% | 24.8\% | 23.4\% |  |  |  |  |  |  |  |

* Includes the effect Federal Grants

Components of Lawrence's Pension Expense for the Fiscal Year Ended June 30, 2017 [GASB 68, Paragraph 33]

| NOTE* | Description | Fiscal 2017 |
| :---: | :--- | ---: |
| A | Service Cost | $\$, 737,363$ |
| A, B | Interest on the Total Pension Liability | $31,842,170$ |
| C | Differences between Expected and Actual Experience | $(1,677,329)$ |
| D | Changes of Assumptions | 0 |
| D | Changes to Benefit Provisions | 0 |
| A | Employee Contributions | $(6,851,473)$ |
| E | Projected Earnings on Pension Plan Investments | $(14,016,932)$ |
| F | Differences between Projected and Actual Earnings on | $2,874,455$ |
| A | Plan Investments | Pension Plan Administrative Expense |
| A | Other Changes in Fiduciary Net Position | 472,754 |
|  | Total Pension Expense | 0 |

* Notes shown on following page. Amounts are based on the following dates:
- Valuation date: January 1 ; Measurement date: December 31 ; Reporting date: following June 30

CHANGES IN METHODS, ASSUMPTIONS, AND PLAN PROVISIONS
The assumptions and methods used to generate these exhibits are consistent with those used in the January 1, 2016 actuarial valuation of Lawrence performed by Stone Consulting, Inc. unless otherwise noted.

## RESULTS BY EMPLOYER

Exhibits are provided beginning on page 12 which provide individual results for the various employers that make up the Lawrence Retirement System. Pension expense, deferred inflows and outflows of resources, and any excess contribution resulting from Federal Grants have been allocated to the various employers in the same manner as the FY2017 appropriation. However, per GASB 68, the change in proportionality from FY2016 to FY2017 if the individual employers' NPL and deferred inflows and outflows need to be allocated to the individual employers. This is calculated on page 14. These amounts are then recognized over the average working lifetime, which is 6.9 years.

## NOTES

A. See the RSI schedule of changes to the net pension liability, on page 1 .
B. Events that impact the total pension liability are assumed to happen evenly throughout the period. In addition, the amount of interest on the total pension liability is calculated using an interest rate equal to the discount rate that was used to determine the service cost. The amount is determined as follows:

| Description | Amount for <br> Period <br> (a) | Portion of <br> Period <br> (b) | Interest <br> Rate <br> (c) | Interest on the Total <br> Pension Liability <br> (a) $\times($ (b) $\times$ (c) |
| :--- | :---: | :---: | :---: | :---: |
| Beginning total pension liability | $\$ 415,175,624$ | $100 \%$ | $7.75 \%$ | $\$ 82,176,111$ |
| Service cost | $8,737,363$ | $100 \%$ | $7.75 \%$ | 677,146 |
| Benefit payments | $(26,092,541)$ | $50 \%$ | $7.75 \%$ | $(1,011,086)$ |
| Total interest on the net pension liability |  |  | $\$ 31,842,170$ |  |

C. Differences between expected and actual experience recognized in the current period in accordance with paragraph 33a of Statement 68. For the detailed calculation of this amount, see the schedules on page 9.
D. Assumption and plan provision changes recognized in pension expense in the current period in accordance with paragraph 33a of Statement 68. For detailed calculation of these amounts, see the schedule on page 9.
E. Changes in the amounts invested are assumed to occur evenly throughout the period. In addition, the amount of projected earnings on pension plan investments is calculated using the assumed rate of return on pension plan investments as of the beginning of the period. The amount is determined as follows:

| Description | Amount for Period <br> (a) | Portion of <br> Period <br> (b) | Projected <br> Rate of Return <br> (c) | Projected Earnings <br> (a) $\times$ (b) $\times$ (c) |
| :--- | ---: | :---: | :---: | ---: |
| Beginning plan fiduciary net <br> position | $\$ 182,660,273$ | $100 \%$ | $7.75 \%$ | $\$ 14,156,171$ |
| Employer contributions (August 1) | $19,329,195$ | $41.7 \%$ | $7.75 \%$ | 624,671 |
| Employee contributions | $6,851,473$ | $50 \%$ | $7.75 \%$ | 265,495 |
| Benefit payments, including <br> refunds of employee contributions | $(26,092,541)$ | $50 \%$ | $7.75 \%$ | $(1,011,086)$ |
| Administrative expense and other | $(472,754)$ | $50 \%$ | $7.75 \%$ | $(18,319)$ |
| Total projected earnings |  |  |  |  |

F. Differences between projected and actual earnings recognized in the current period in accordance with paragraph 33b of Statement 68. For detailed calculation of this amount, see the schedule on page 9.

Increase / (Decrease) in Pension Expense Arising from the Recognition of the Effects of Differences between Expected and Actual Experience


Increase / (Decrease) in Pension Expense Arising from the Recognition of the Effects of Changes of Assumptions

| Year |  |  | Recognition period (years) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2014 | \$ | - | 0 | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - |
| 2015 | \$ | - | 6.9 | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - |
| 2016 | \$ | - | 6.9 | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - |
| 2017 | \$ | - | 6.9 | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - |
| Net increase (decrease) in pension expense |  |  |  | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - |

Increase / (Decrease) in Pension Expense Arising from the Recognition of Differences between Expected and Actual Earnings on Pension Plan Investments

| Year |  | en projected nings on vestments | Recognition period (years) |  | 2015 |  | 2016 |  | 2017 |  | 2018 |  | 2019 |  | 2020 |  | 2021 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2014 | \$ | - | 5 | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - |
| 2015 | \$ | 523,278 | 5 | \$ | 104,656 | \$ | 104,656 | \$ | 104,656 | \$ | 104,656 | \$ | 104,656 | \$ | - | \$ | - |
| 2016 | \$ | 13,022,328 | 5 | \$ | - | \$ | 2,604,466 | \$ | 2,604,466 | \$ | 2,604,466 | \$ | 2,604,466 | \$ | 2,604,466 | \$ | - |
| 2017 | \$ | 826,668 | 5 | \$ | - | \$ | - | \$ | 165,334 | \$ | 165,334 | \$ | 165,334 | \$ | 165,334 | \$ | 165,334 |
| Net increase (decrease) in pension expense |  |  |  | \$ | 104,656 | \$ | 2,709,121 | \$ | 2,874,455 | \$ | 2,874,455 | \$ | 2,874,455 | \$ | 2,769,799 | \$ | 165,334 |

Deferred Outflows and Deferred Inflows of Resources Arising from Differences between Expected and Actual Experience

|  |  |  |  |  |  |  | BALANCES AT JUNE 30, 2017 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year | Experience Losses <br> (a) |  | Experience Gains <br> (b) |  | Amounts Recognized in Pension Expense through June 30, 2017 <br> (c) |  | Deferred Outflows of Resources <br> (a) - (c) |  | Deferred Inflows of Resources <br> (b) - (c) |  |
| 2015 | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - |
| 2016 | \$ | - | \$ | - | \$ | - | \$ | - | \$ | - |
| 2017 | \$ | - | \$ | $(11,573,571)$ | \$ | $(1,677,329)$ | \$ | - | \$ | (9,896,242) |
| TOTAL |  |  |  |  |  |  | \$ | - | \$ | $(9,896,242)$ |

## Deferred Outflows and Deferred Inflows of Resources Arising from Changes of Assumptions

|  |  |  |  | BALAN JUNE 30 | $\begin{aligned} & \text { CES AT } \\ & , 2017 \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Year | Increases in the Total Pension Liability <br> (a) | Decreases in the Total Pension Lability <br> (b) | Amounts Recognized in Pension Expense through June 30, 2017 <br> (c) | Deferred Outflows of Resources <br> (a) - (c) | Deferred Inflows of Resources <br> (b) - (c) |
| 2015 | \$ - | \$ - | \$ | \$ - | \$ |
| 2016 | \$ - | \$ | \$ | \$ | \$ |
| 2017 | \$ - | \$ | \$ | \$ | \$ |
| TOTAL |  |  |  | \$ | \$ - |

## Deferred Outflows and Deferred Inflows of Resources

Arising from Differences between Expected and Actual Earnings on Pension Plan Investments

|  |  |  |  |  |  |  |  | BALA <br> JUNE |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Year |  | nt Earnings Projected <br> (a) |  |  |  | in Pension $\text { 30, } 2017$ |  | d Outflows esources - (c) |  | ows S |
| 2015 | \$ | 523,278 | \$ | - | \$ | 313,967 | \$ | 209,311 | \$ | - |
| 2016 | \$ | 13,022,328 | \$ | - | \$ | 5,208,931 | \$ | 7,813,397 | \$ | - |
| 2017 | \$ | 826,668 | \$ | - | \$ | 165,334 | \$ | 661,334 | \$ | - |
| TOTAL |  |  |  |  |  |  | \$ | 8,684,042 | \$ | - |
| NET TOTAL |  |  |  |  |  |  | \$ | \$ 8,684,042 |  |  |


| Starting Value*$(12 / 31 / 2015)$ | NET INVESTMENT AMOUNTS |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Beginning of month |  | Middle of Month | End of Month | Periods Invested** | Investment with Interest |  |
|  | \$ | 183,028,850.92 |  |  | 12 | \$ | 196,809,198.29 |
| Cash Flows: |  |  |  |  |  |  |  |
| January |  | 253,083.34 | 242,600.49 | -1,895,410.55 | 11 |  | (1,493,608.93) |
| February |  | 213,396.77 | 228,922.29 | -2,120,537.90 | 10 |  | (1,780,759.60) |
| March |  | 169,798.95 | 250,508.69 | -1,887,660.02 | 9 |  | (1,547,565.19) |
| April |  | 267,194.91 | 18,650.20 | -1,871,552.66 | 8 |  | (1,662,572.46) |
| May |  | 350,089.31 | 10,999.72 | -1,902,733.63 | 7 |  | (1,606,076.11) |
| June |  | 249,670.53 | 270,422.39 | -2,074,190.86 | 6 |  | $(1,609,120.47)$ |
| July |  | 219,387.20 | 162,876.89 | -1,749,088.33 | 5 |  | (1,406,916.50) |
| August |  | 16,901,601.67 | 171,822.57 | -3,174,267.75 | 4 |  | 14,345,172.71 |
| September |  | -8,794.76 | 0.00 | -292,128.28 | 3 |  | $(306,488.30)$ |
| October |  | 241,751.22 | 140,588.40 | -2,125,840.92 | 2 |  | (1,762,807.39) |
| November |  | 1,225,371.34 | 298,559.34 | -2,151,500.21 | 1 |  | (622,987.32) |
| December |  | 454,958.11 | 316,181.47 | -1,709,639.73 | 0 |  | (934,781.88) |
| Ending Value*$(12 / 31 / 2016)$ | \$196,420,686.85 |  |  |  | Sum: | \$ | 196,420,686.85 |
|  | * Value shown does not include any payables or receiveables, except those related to investments. <br> ** Middle of period cash flows are given an additional half period of interest, and beginning of period cash flows are given an additional full period. |  |  |  |  |  |  |
|  | Return Rate: |  | 7.53\% |  |  |  |  |


|  | Covered Payroll＊ |  | Proportionate <br> Share of NPL＊＊ |  |  | Proportionate share of NPL Discount Sensitivity |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Employer |  |  | Proportionate share of NPL as a percentage of covered payroll＊ |  | 1\％Increase (8.75\%) |  | $\begin{gathered} \text { 1\% Decrease } \\ \text { (6.75\%) } \end{gathered}$ |
| City of Lawrence | \＄ | 67，134，686 |  |  | \＄ | 201，674，657 | 300．4\％ | \＄ | 167，547，610 | \＄ | 247，480，062 |
| Greater Lawrence Regional Vocational Tech | \＄ | 3，192，799 | \＄ | 9，610，040 | 301．0\％ | \＄ | 7，980，462 | \＄ | 11，797，263 |
| Lawrence Housing Authority | \＄ | 3，179，804 | \＄ | 9，990，060 | 314．2\％ | \＄ | 8，240，051 | \＄ | 12，338，925 |
| M．V．R．T．A． | \＄ | 234，353 | \＄ | 1，348，379 | 575．4\％ | \＄ | 1，220，421 | \＄ | 1，520，124 |
| TOTAL | \＄ | 73，741，641 | \＄ | 222，623，135 | 301．9\％ | \＄ | 184，988，544 |  | 273，136，374 |


| Employer |  | Actuarially determined contribution FY2017 | Contributions made FY 2017 |  | Contribution deficiency （excess） |  | Contributions as a percentage of covered payroll＊＊＊ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| City of Lawrence | \＄ | 17，409，358 | \＄ | $(17,417,550)$ | \＄ | $(8,192)$ | 25．3\％ |
| Greater Lawrence Regional Vocational Tech | \＄ | 829，064 | \＄ | $(829,455)$ | \＄ | （391） | 25．3\％ |
| Lawrence Housing Authority | \＄ | 853，241 | \＄ | $(853,661)$ | \＄ | （420） | 26．3\％ |
| M．V．R．T．A． | \＄ | 228，498 | \＄ | $(228,529)$ | \＄ | （31） | 95．7\％ |
| TOTAL | \＄ | 19，320，161 | \＄ | $(19,329,195)$ | \＄ | $(9,034)$ | 25．6\％ |


| Employer | Proportion | Proportionate Share of Pension Expense |  | Proportion changes and differences between employer contributions and proportionate share recognized as expense |  |  | Total <br> Pension <br> Expense |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| City of Lawrence | 90．68\％ | \＄ | 19，369，090 | \＄ | $(130,070)$ | \＄ | 19，239，020 |
| Greater Lawrence Regional Vocational Tech | 4．33\％ | \＄ | 922，960 | \＄ | 79，389 | \＄ | 1，002，349 |
| Lawrence Housing Authority | 4．65\％ | \＄ | 959，458 | \＄ | $(52,055)$ | \＄ | 907，403 |
| M．V．R．T．A． | 0．34\％ | \＄ | 129，500 | \＄ | 102，736 | \＄ | 232，236 |
| TOTAL | 100．00\％ | \＄ | 21，381，008 |  |  |  |  |

＊Covered Payroll is the projected amount for the 2016 calendar year based on employee data as of December 31， 2015
${ }^{* *}$ ERI liabiltiy used in the proprtionate share of NPL is $\$ 7,696,638$ for City，$\$ 347,525$ for GLRVT，$\$ 43,017$ for Housing，and a present value of $\$ 621,068$ for payments to be made by the MVRTA for service awarded through a decision by the
Contributory Retirement Appeals Board（CRAB）．This methodology assumes that the MVRTA have not accounted for these
payments on their Financial Statement as a separate liability．
＊＊＊Here the Covered Payroll figure is projected for Fiscal Year 2017，based on employee data as of December 31， 2015

Deferred Outflows of Resources by Employer*

| Employer | Differences between expected and actual experience | Changes of assumptions | Net difference between projected and actual earnings on pension plan investments | Changes in proportion and differences between employer contributions and proportionate share of contributions | Employer contributions subsequent to the measurement date | Total Deferred Outtlows of Resources |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| City of Lawrence | \$ | \$ | \$ 7,864,448 | \$ 104,161 | \$ - | \$ 7,968,609 |
| Greater Lawrence Regional Vocational Tech | \$ | \$ - | 374,750 | \$ 663,158 | \$ - | \$ 1,037,909 |
| Lawrence Housing Authority | \$ | \$ | \$ 389,565 | \$ 59,521 | \$ | \$ 449,086 |
| M. V. R.T. A. | \$ | \$ | \$ 55,279 | \$ 659,601 | \$ - | \$ 714,880 |
| TOTAL | \$ | \$ | \$ 8,684,042 | \$ 1,486,441 | \$ | \$ 10,170,483 |

Deferred Inflows of Resources by Employer*

| Employer | Differences between expected and actual experience |  | Changes of assumptions |  | Net difference between projected and actual earnings on pension plan investments |  | Changes in proportion and differences between employer contributions and proportionate share of contributions |  | Employer contributions subsequent to the measurement date | Total Deferred Inflows of Resources |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| City of Lawrence | \$ | 8,962,241 | \$ | - | \$ | - | \$ | 941,472 | N/A | \$ | 9,903,713 |
| Greater Lawrence Regional Vocational Tech | \$ | 427,061 | \$ | - | \$ | - | \$ | 163,682 | N/A | \$ | 590,743 |
| Lawrence Housing Authority | \$ | 443,944 | \$ | - | \$ | - | \$ | 381,287 | N/A | \$ | 825,232 |
| M. V. R. T. A. | \$ | 62,995 | \$ | - | \$ | - | \$ | - | N/A | \$ | 62,995 |
| TOTAL | \$ | 9,896,242 | \$ | - | \$ | - | \$ | 1,486,441 | N/A |  | 11,382,683 |

Recognition of Deferred Outflows and Deferred Inflows

| Employer | AMOUNT TO BE RECOGNIZED FOR THE YEAR ENDING DECEMBER 31, |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2017 |  | 2018 |  | 2019 |  | 2020 |  | 2021 |  | Thereafter |  |
| City of Lawrence | \$ | 945,827 | \$ | 945,827 | \$ | 851,049 | \$ | $(1,507,609)$ | \$ | $(1,659,464)$ | \$ | (1,510,736) |
| Greater Lawrence Regional Vocational Tech | \$ | 130,656 | \$ | 130,656 | \$ | 126,140 | \$ | 13,747 | \$ | 9,953 | \$ | 36,015 |
| Lawrence Housing Authority | \$ | 1,225 | \$ | 1,225 | \$ | $(3,470)$ | \$ | $(120,306)$ | \$ | $(128,937)$ | \$ | $(125,883)$ |
| M. V. R. T. A. | \$ | 119,417 | \$ | 119,417 | \$ | 118,751 | \$ | 102,172 | \$ | 101,120 | \$ | 91,008 |
| TOTAL | \$ | 1,197,125 | \$ | 1,197,125 | \$ | 1,092,470 | \$ | $(1,511,996)$ | \$ | $(1,677,329)$ | \$ | $(1,509,596)$ |

* Deferred Outflows and Inflows due to experience, assumptions, and investemnt retrun are allocated to each employer according to their proprtion of the NPL

Effects of Changes in Proportion on Employers' Proportionate Share of NPL, and Deferred Inflows and Deferred Outflows of Resources

|  | Proportion Change |  |  |  |  |  | FY2017 Contribution |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Employer | Prior Proportionate Share of Prior NPL net of Deferrals |  | Share of Prior NPL based on Current Proportion of NPL |  | Difference <br> (A) |  | Proportionate Share of Contribution based on Share of NPL |  | Amount Paid |  | Difference <br> (B) |  |
| City of Lawrence | \$ | 201,865,411 | \$ | 200,851,735 | \$ | $(1,013,676)$ | \$ | 17,504,918 | \$ | 17,417,550 | \$ | $(87,368)$ |
| Greater Lawrence Regional Vocational Tech | \$ | 8,790,588 | \$ | 9,570,820 | \$ | 780,233 | \$ | 834,130 | \$ | 829,455 | \$ | $(4,675)$ |
| Lawrence Housing Authority | \$ | 10,381,654 | \$ | 9,949,187 | \$ | $(432,467)$ | \$ | 867,106 | \$ | 853,661 | \$ | $(13,445)$ |
| M. V. R. T. A. | \$ | 745,869 | \$ | 1,411,780 | \$ | 665,910 | \$ | 123,041 | \$ | 228,529 | \$ | 105,487 |
| TOTAL | \$ | 221,783,522 | \$ | 221,783,522 | \$ | - | \$ | 19,329,195 | \$ | 19,329,195 | \$ | - |


| Employer |  | Total Proportion Change $(A)+(B)$ | Recognized as Pension Expense* |  | Deferred for later recognition |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| City of Lawrence | \$ | $(1,101,044)$ | \$ | $(159,572)$ | \$ | $(941,472)$ |
| Greater Lawrence Regional Vocational Tech | \$ | 775,558 | \$ | 112,400 | \$ | 663,158 |
| Lawrence Housing Authority | \$ | $(445,912)$ | \$ | $(64,625)$ | \$ | $(381,287)$ |
| M. V. R. T. A. | \$ | 771,398 | \$ | 111,797 | \$ | 659,601 |
| TOTAL | \$ | - | \$ | - | \$ | - |

* Based on an average remaining service life of 6.9 years.


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[^1]:    Note: sums may not total due to rounding

